

IE-231 Homework 1

Due Date Apr 4, 2017, 09:00

- This is a double-sized group homework (i.e. it counts as 2 homeworks).
- There are 10 questions, each 20pts. You should answer 5 questions (indicate the question numbers clearly). Rest of them are exercise.
- If you submit more than 5 answers only the first 5 will be graded.
- Your groups should be the same as the In Class Assignments. Write your group number and student name/surname as well. Students that do not belong in their groups will not get points.
- Your answers should be handwritten (no R Markdown). Show your work.
- You should submit your work by the start of the midterm.

Question 1

How many ways are there to arrange “ECONOMETRICS”.

- a) In any order.
- b) Vowels together.
- c) No consecutive vowels.

Question 2

7 people from Istanbul (suppose names A-B-C-D-E-F-G) and 7 people from Ankara (M-N-O-P-Q-R-S) will sit around a round table.

- a) In how many different ways can they sit around the table?
- b) Same as (a) but no two people from Ankara should sit together.
- c) Same as (a) but all the people from Istanbul should sit together.

Question 3

You roll a die once, and assume the number you rolled is X . Then continue rolling the die until you either match or exceed X . What is the expected number of additional rolls?

Question 4

In a three dice roll, if at least two dice have the same number (e.g. 5-5-4 or 3-3-3) you win.

- a) What is the probability that you win at least three times in a 30 rolls game?
- b) What is the expected number and variance of the number of wins?

Question 5

In a Go game, a player that wins three games out of five is the winner. Suppose the artificial intelligence Alpha Go has probability 0.65 of winning against the World's (Human) Go Champion. What is the probability that Alpha Go wins the game at the 4th game?

Question 6

An egg basket contains 8 eggs, 4 of which are broken. 3 eggs are selected to make an omelette.

- What is the probability that all 3 eggs are intact?
- What is the probability that the 2nd broken egg is the 3rd egg?

Question 7

Nejat is a film critic and he will attend to IKSV Film Festival between April 5-15. Nejat likes a movie with probability 0.6 if the genre of the movie is mystery. For other genres, he likes the movie with probability 0.4. There will be 40 movies during the festival, 10 of which are mystery.

- What is the probability that Nejat will like a randomly selected movie?
- Suppose Nejat did not like the film. What is the probability that the selected movie is a non-mystery film?

Question 8

A student applies for internships to 11 companies. She has a 0.6 probability to get an offer for an internship.

- What is the probability that she will get offers from at least 4 companies?
- What is the probability that she gets her fourth offer at the seventh application?
- What is the expected value and variance of the applications?

Question 9

A steakhouse serves (C)hateaubriand, (K)obe Beef Tenderloin and (T)-Bone. Customers order C with probability 0.35, K w.p. 0.2 and T w.p. 0.45.

- 12 customers arrive. What is the probability that 4 of them order C, 3 order K and 5 order T?
- Suppose C sells for 90TL, K for 150TL and T for 120TL. If 100 customers are served that day, what is the expected revenue?

Question 10

An international student group will select a committee of 4 people at random. There are 7 Turkish, 6 Greek, 4 Italian and 5 Irish students in the group.

- What is the probability that all countries are represented?
- If the committee consisted of 5 people what would be the probability of (a)?